# ENAE788M Assignment 4a - Estimating 3D trajectory of a stereo sensor

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## I. INTRODUCTION

This project involves the estimating the 3D camera trajectory of a stereo sensor. The stereo camera data bag files provided by team BRZ is taken as input for estimating the 3D camera trajectory.

#### **II. FEATURE MATCHING**

The first step involves acquiring the left and right images of the stereo sensor. These are got by subscribing to topics "/duo3d/left/image\_rect" and "/duo3d/right/image\_rect" for the left and right images respectively. Once the images are acquired, feature points are extracted from the left and right images using the Features from Accelerated Segment Test (FAST) algorithm. The feature points from the left and right images are brute forced compared using the L2 norm to find matching features. The matching features are sorted by closest match and then only the first few (5 to be exact) are used for depth estimation.



**Fig. 1:** Features obtained from the FAST algorithm in the two images obtained from the stereo camera.

#### **III. DEPTH ESTIMATION**

For depth estimation, the disparity of each of the first five matches is calculated. The disparity is calculated using the equation (1)

$$d = (X_{CL} - X_L) - (X_{CR} - X_R)$$
(1)

where  $X_{CL}$  is x-pixel coordinate of center of left Image,  $X_L$  is x-pixel coordinate of feature point in left image,  $X_{CR}$  is x-pixel coordinate of right image and  $X_R$  is x-pixel coordinate of feature point in right image. Once the disparity d is calculated, the depth is determined using the equation (2):

$$Z = f_P B/d \tag{2}$$

where Z is the depth,  $f_P$  is the focal length in pixel units, B is the baseline distance and d is the disparity. Using the Duo3d MLX datasheet, the focal length f=2mm and the baseline distance d=30 mm. The focal length  $f_P$  is calculated as f/w where w is the pixel width (in physical units) obtained as  $6\mu m$  from DUO 3D datasheet.

The average of the depth calculated from the best 5 matched points is determined and run through a 3-point moving average low pass filter to filter out high frequency noise. It is observed through testing that were a some bias error of 30 cm associated with the calculated depth. This bias value is subtracted from the filtered Z value to get final Z depth estimate.

## IV. OPTICAL FLOW

In order to estimate the linear and angular velocities, the sparse optical flow between two consecutive frames is computed using the Kanade-Lucas-Tomasi Tracker (KLT). First, corner points are detected using the function from OpenCV, *goodFeaturesToTrack*. This function is an implementation of the Shi-Tomasi corner detection, in which we set the maximum number of corners that should be detected to 100, the quality level of detection to 0.3, the minimum distance between detected corners to 10, and the block size to 10. Once we have the corner points, we then pass them to the OpenCV function *calcOpticalFlowPyrLK* along with two consecutive frames to return the positions of the detected corner in the both images. In Figs. 2-4, we can observe the tracks generated from the optical flow computed.



**Fig. 2:** Corner points detected using the KLT algorithm. Gray and black circles represent these corner points detected in the first left image of the stereo camera.

Once we have the corresponding positions of corner points in the consecutive images, we then compute the delta time  $\Delta t$  by extracting the timestamp from each image. With the



**Fig. 3:** Tracks obtained from the optical flow using the corner points detected after 10 frames.



**Fig. 4:** Tracks obtained from the optical flow using the corner points detected after 50 frames.

command rostopic hz, we were able to get the publish rate, which was about 14Hz (or 0.07 secs).

The corner points detected in consecutive frames are transformed from pixel values to normalized coordinates by dividing these values by the focal length in pixels. Then, we compute their displacement and divide it by the delta time between the consecutive frames.

The next step is to use these normalized coordinates along with the optical flow equation to solve for the linear and angular velocities:

$$\begin{bmatrix} \dot{x}\\ \dot{y} \end{bmatrix} = \begin{bmatrix} -\frac{1}{z} & 0 & \frac{x}{z} & xy & -(1+x^2) & y\\ 0 & -\frac{1}{z} & \frac{y}{z} & (1+y^2) & -xy & -x \end{bmatrix} \begin{bmatrix} V_x\\ V_y\\ V_z\\ \Omega_x\\ \Omega_y\\ \Omega_z \end{bmatrix}$$

Using the function *lstsq* from the *numpy* package, we compute the linear and angular velocities for each pair of detected corners between consecutive frames. We integrate the velocities obtained over the delta time and compute a

pose estimate. In order to improve accuracy in the estimates, we identify outliers by computing the median value of the estimates and the absolute difference between the estimates and their median. We then keep the estimates that are within a small deviation from the median.

For the final step, we average out the pose estimates after removing the outliers and this average estimate is added to the current pose which is assumed to start at **0**.

#### V. RVIZ DISPLAY

We use Rviz application to plot the pose positions of the quadrotor wrto to the world frame. The pose estimates calculated using optical flow and depth estimation is broadcasted from our application to Rviz every 0.1 sec. For recording the video for rviz and detected features, a time scaling factor of 4 is multiplied to  $\Delta t$ . This is done for both helix and point 2 point trajectory. This constant can be considered as a gain that drives us closer to the odometry trajectory. The recorded videos are speed up 4-5 times its initial speed to limit the size of the video.



Fig. 5

### VI. CONCLUSION

In this project, we did pose estimation using stereo camera. We used feature detection using FAST algorithm to estimate depth and optical flow to estimate the rotation and translation. Our pose estimation produced correct shapes for helix and point to point trajectory but our estimation of magnitudes of the pose could have improved. Our future work will primarily include adding more support to remove outleirs and just using optical flow to estimate depth (instead of manually do it through FAST algorithm).